

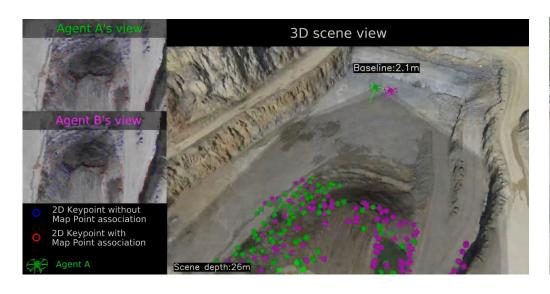
# **Towards Asynchronous SLAM with Event Cameras**

### Ignacio Alzugaray

Vision for Robotics Lab, ETH Zurich



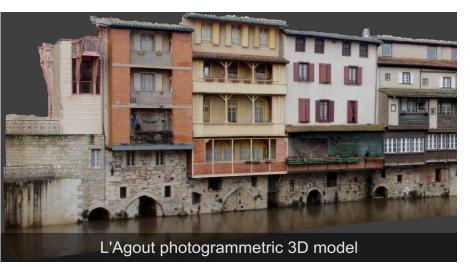
### Research @ Vision For Robotics Lab





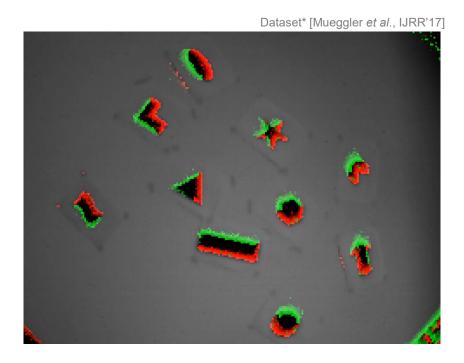
### Robust Perception for Robotics:

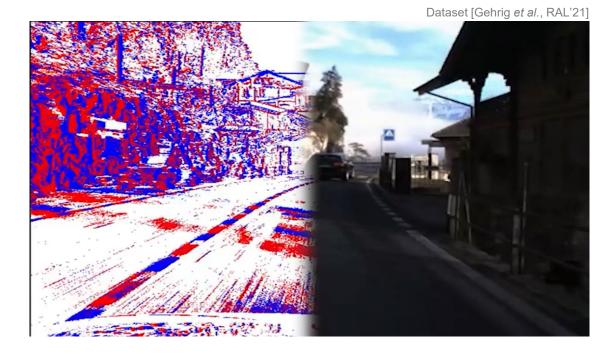
- Multi-Agent Visual SLAM
- Vision-based Navigation & Manipulation
- Viewpoint-tolerant Place Recognition





### **Event Cameras in Robotics Application**



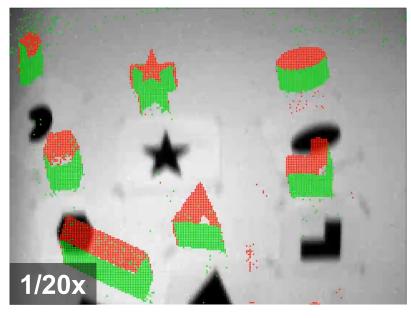


- Sensor: Fast Perception, HDR capabilities, Low Power
- Output: Asynchronous and Sparse

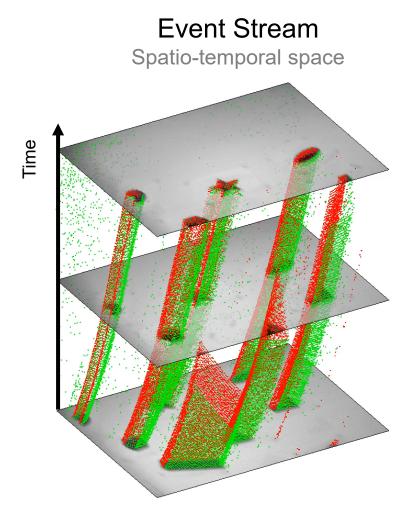


# Asynchronous and Sparse Event Stream

Events
Image plane

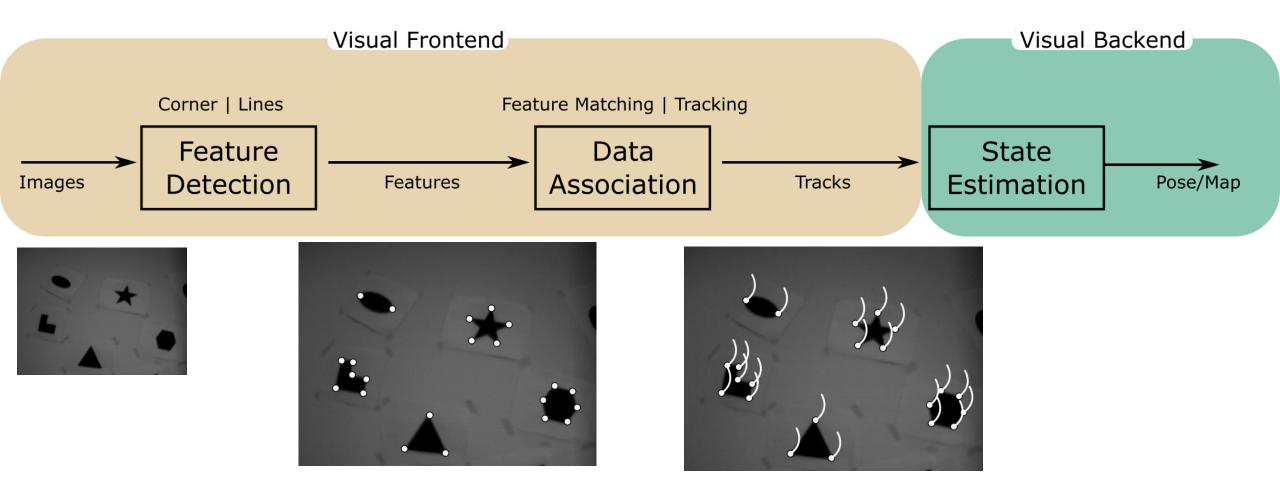


- No notion of time-discretization
- Only intensity changes are captured



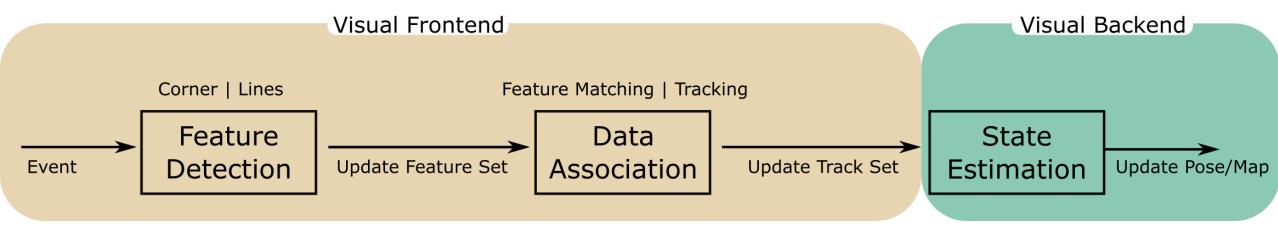


### Traditional Visual SLAM Pipeline

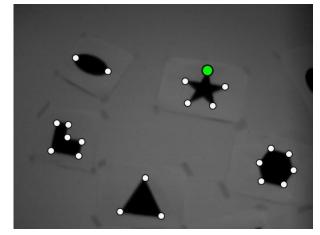


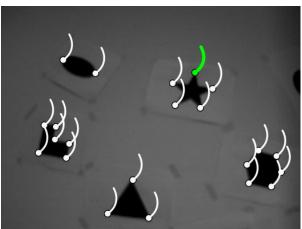


### Asynchronous Event-Driven SLAM Pipeline



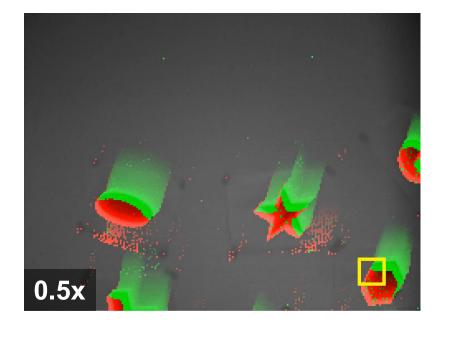




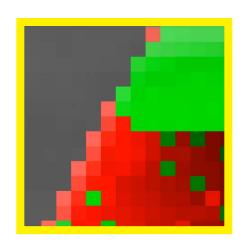




### **Events**

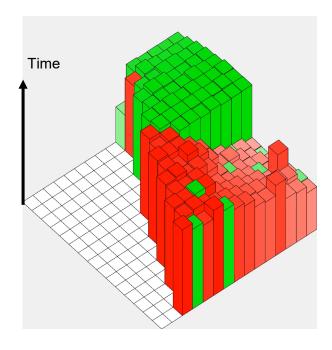


Corner Close-up



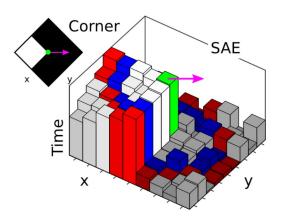
Surface of Active Events

(stores the timestamp of the last event in each location)



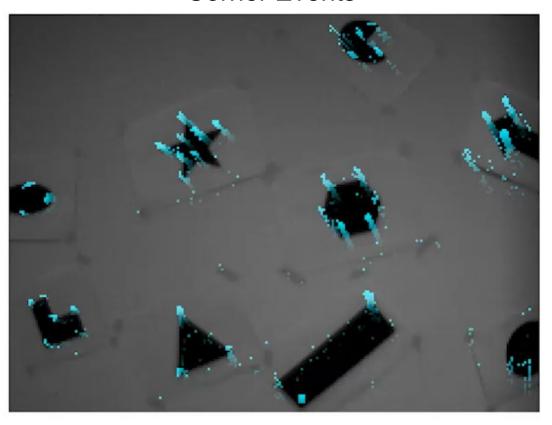


# Events Close-up



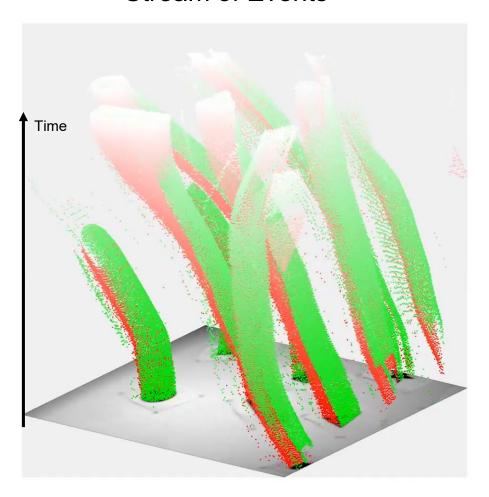
Local Surface of Events (centered at the newest event)

### **Corner Events**

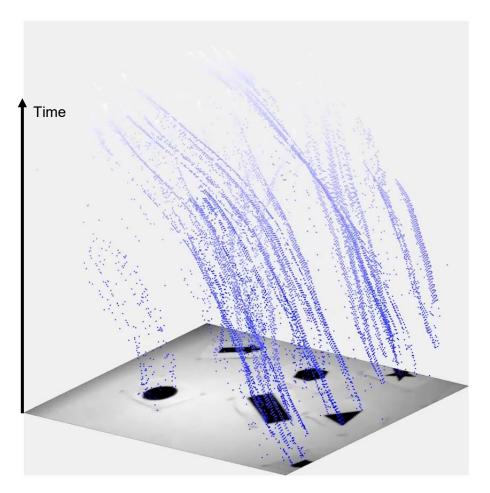




### **Stream of Events**

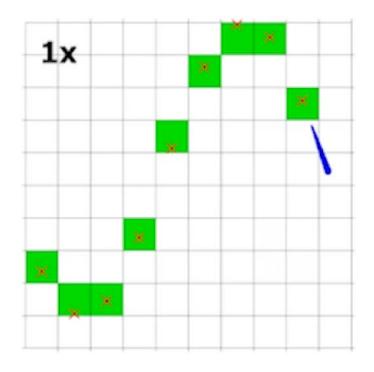


### Stream of Corner Events

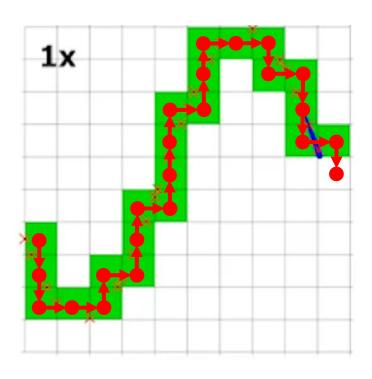


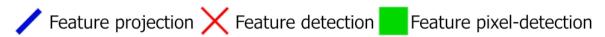


### Frame-based detection



### **Event-driven detection**

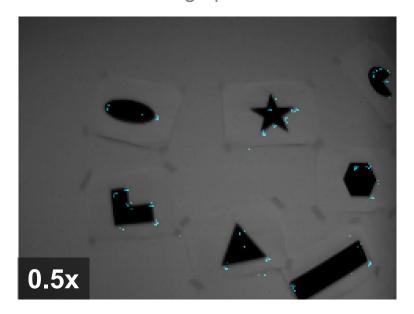


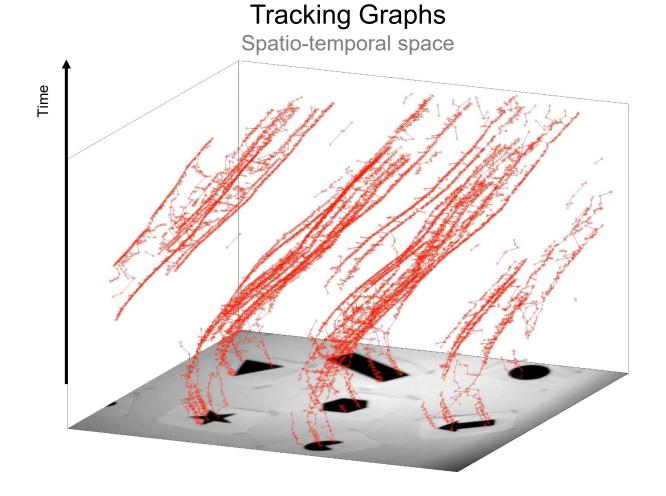


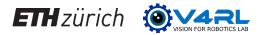


# Naïve Asynchronous Corner Tracking

Corner Events
Image plane

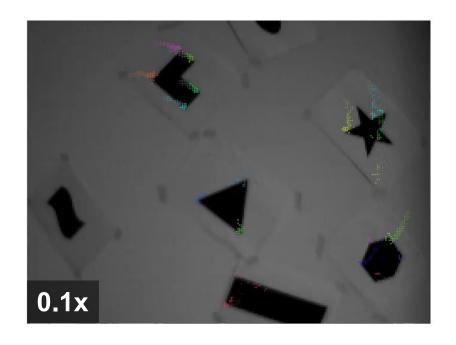






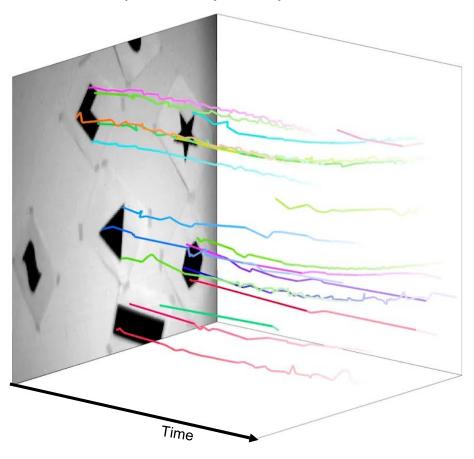
### Naïve Asynchronous Corner Tracking

Corner Tracking Image plane



# Corner Tracking

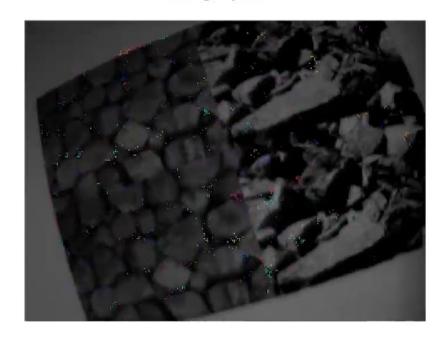
Spatio-temporal space

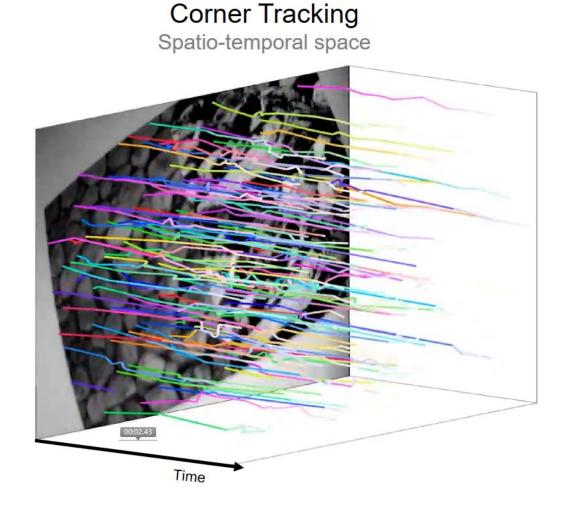


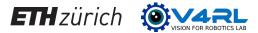


# Naïve Asynchronous Corner Tracking

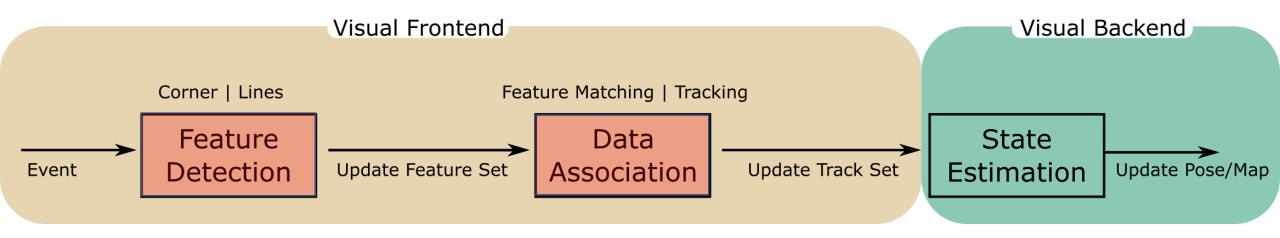
Corner Tracking Image plane





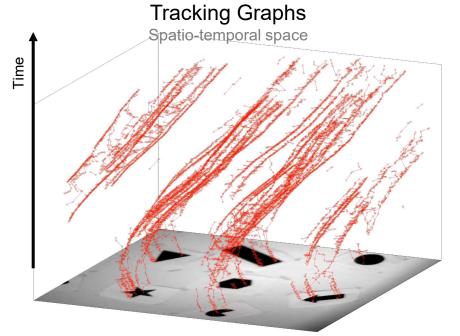


### Asynchronous Event-Driven SLAM Pipeline



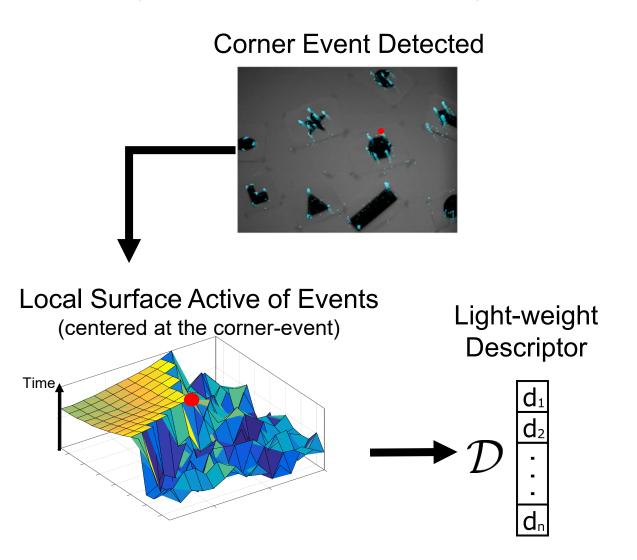
- Event Corner Detection
- · Naïve Event Corner Association
- Offline Corner Tracks Retrieval

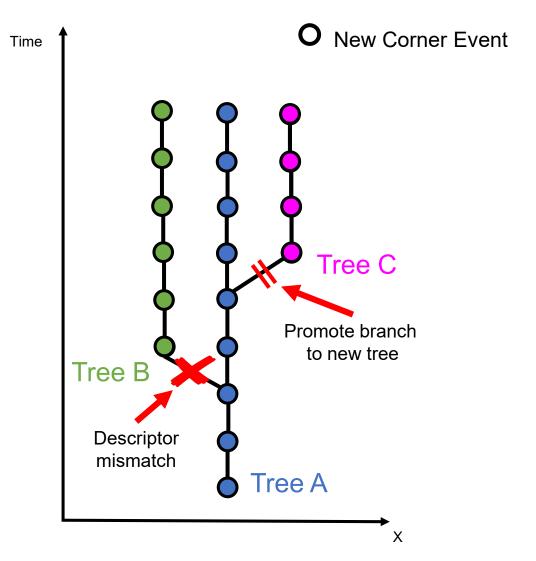
Asynchronous Corner Detection and Tracking for Event Cameras in Real-Time [Alzugaray & Chli, RAL'18]



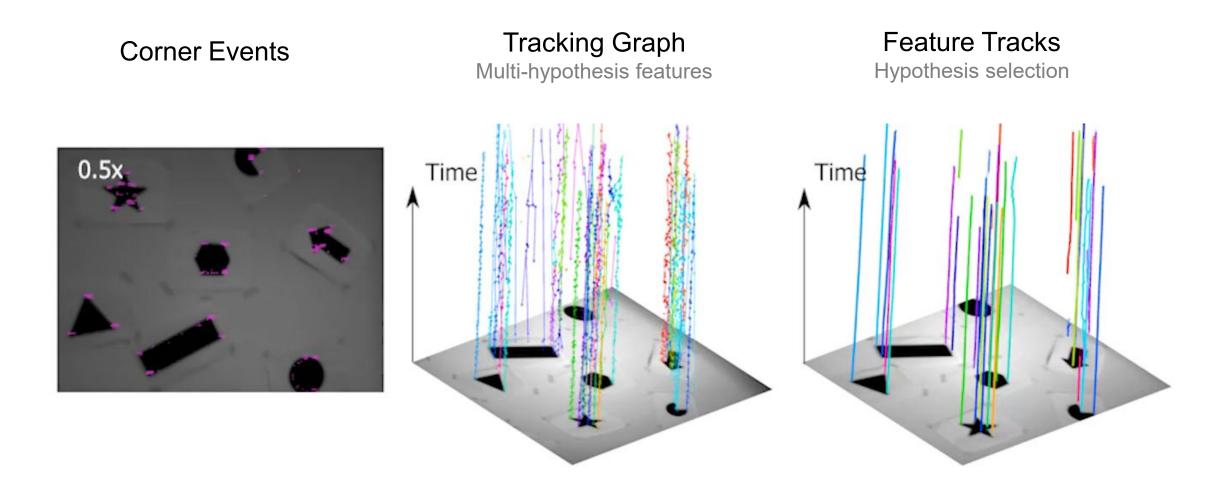
**Unreliable Data Association** 









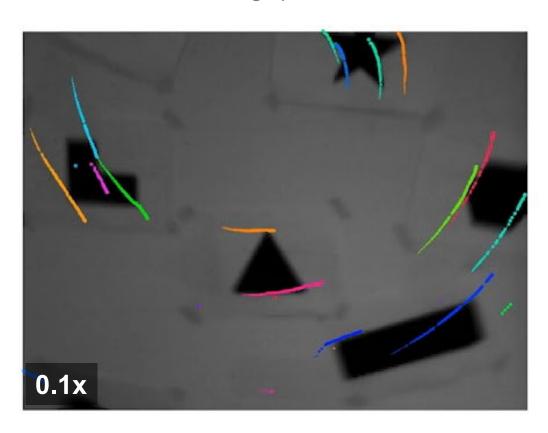


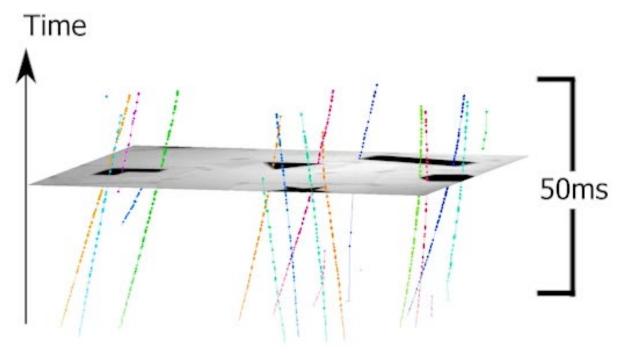


### **Corner Tracking**

Image plane

# Corner Tracking Spatio-temporal space

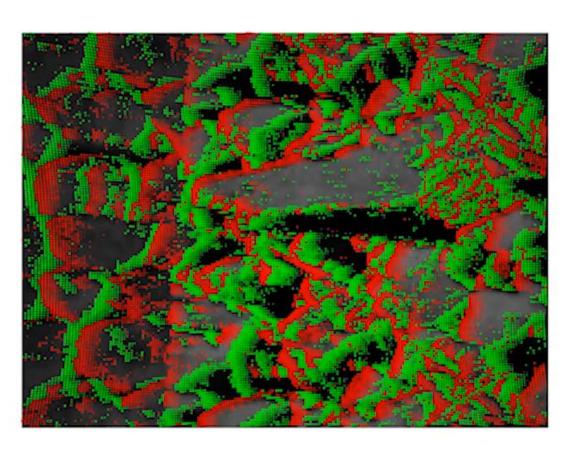


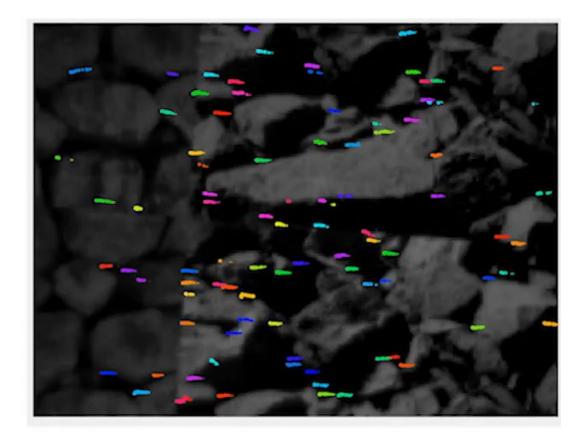




**Events** 

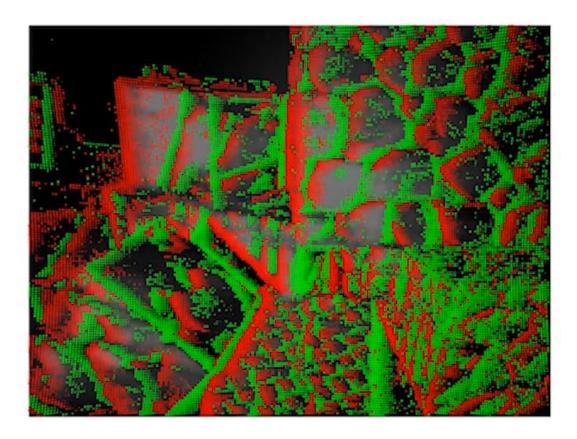
**Corner Tracking** 







**Events** 

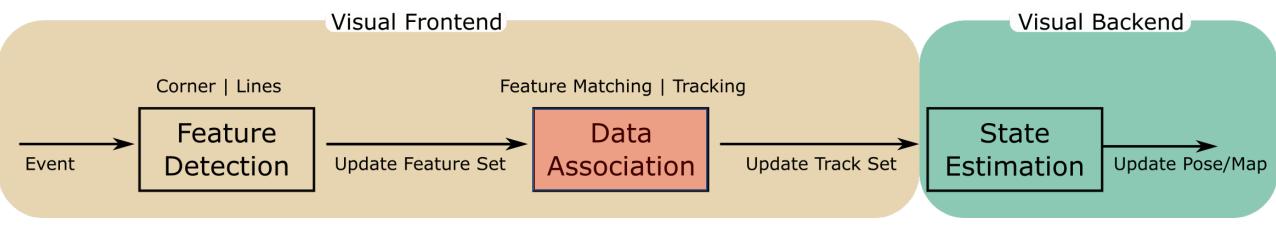


**Corner Tracking** 





### Asynchronous Event-Driven SLAM Pipeline

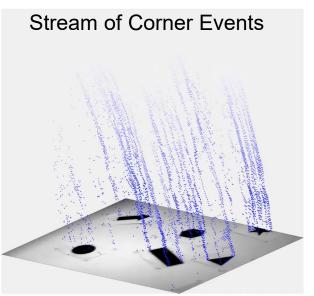


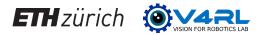
- Event Corner Detection
- Naïve Event Corner Association
- Offline Corner Tracks Retrieval

Asynchronous Corner Detection and Tracking for Event Cameras in Real-Time [Alzugaray & Chli, RAL'18]

- Local Event Descriptor
- Multi-hypothesis Data Association
- Online Corner Track Retrieval

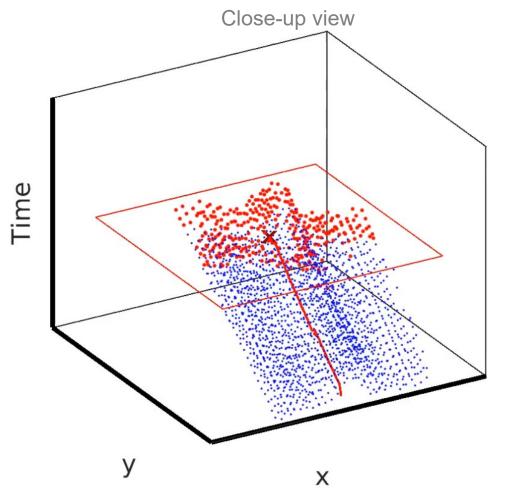
ACE: An Efficient Asynchronous Corner Tracker for Event Cameras [Alzugaray & Chli, 3DV'18]

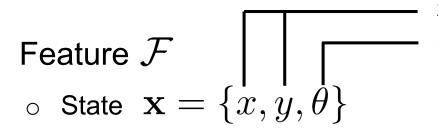




### **Asynchronous Tracking of Events**

### Feature Track in the Event Stream





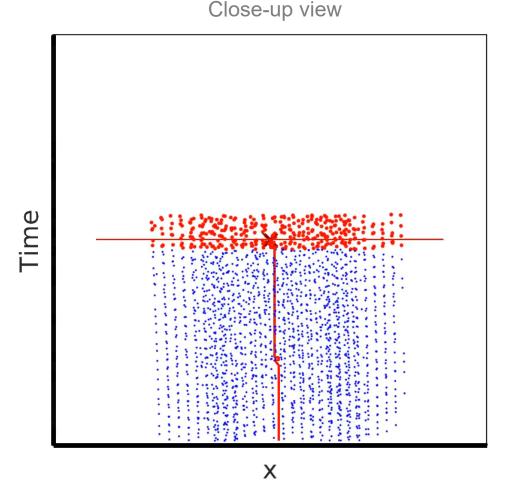
xy-pixel coordinates in-plane orientation

- $\sim$  Window of Latest Events  ${\cal E}$ 
  - Fixed number of events



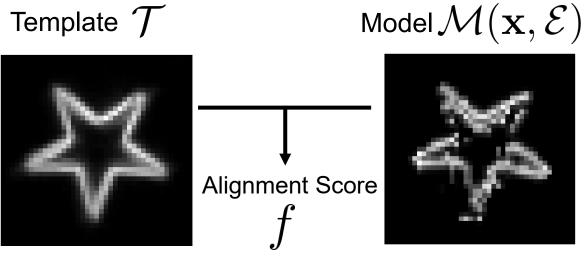
# Asynchronous Tracking of Events

### Feature Track in the Event Stream



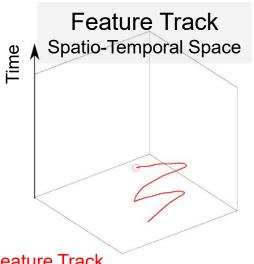
### Feature ${\mathcal F}$

- $\circ$  State  $\mathbf{x} = \{x, y, \theta\}$
- Window of Latest Events  ${\mathcal E}$ 
  - Fixed number of events
- Template  $\mathcal{T}$

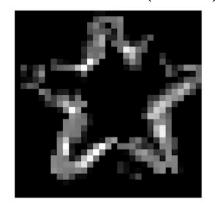




### Feature Tracking as Optimization Problem



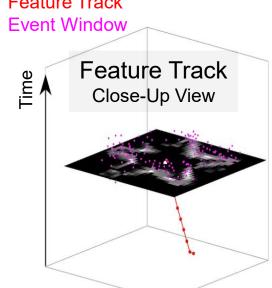




Template  $\mathcal{T}$ 



Feature Track



Alignment Score Function

$$\mathbf{x}^* = rg \max_{\mathbf{x} \in \mathcal{X}} f(\mathbf{x}, \mathcal{E}, \mathcal{T})$$
 $\mathbf{x} \in \mathcal{X}$ 

Optimal Feature State

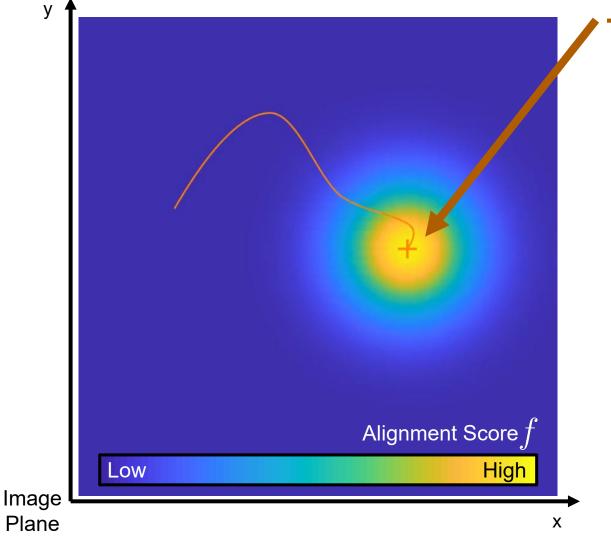
 $\mathbf{x}^* = \mathbf{x} \in \mathcal{X}$ 
 $\mathbf{x} \in \mathcal{X}$ 

Up to Millions of Events per second!

Window of latest events

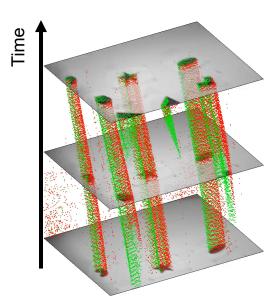


# Feature Tracking with Asynchronous Hypotheses Evaluation



+ Optimal State (Continuous)

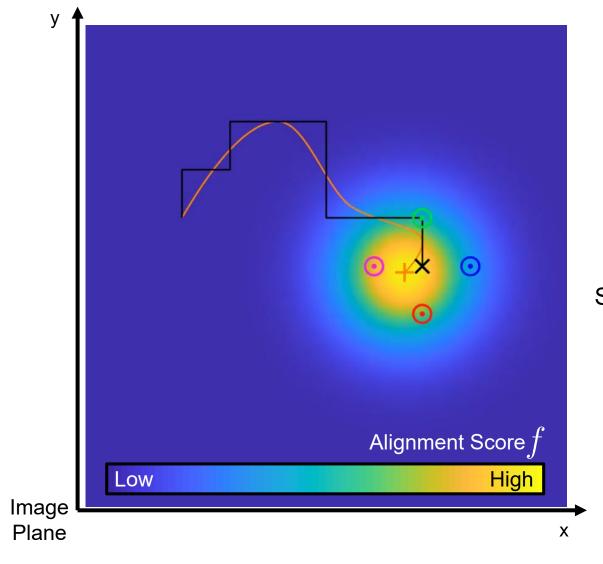
$$\mathbf{x}^{(k+1)} = \underset{\mathbf{x} \in \mathcal{X}}{\operatorname{arg \, max}} \ f(\mathbf{x}, \mathcal{E}^{(k+1)}, \mathcal{T}^{(k+1)})$$



Continuous stream of information



# Feature Tracking with Asynchronous Hypotheses Evaluation



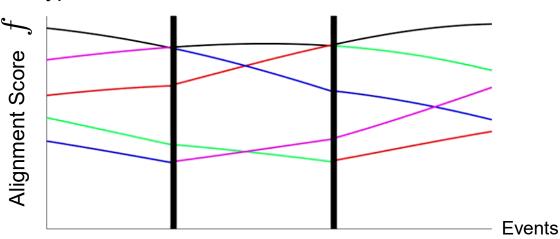
Optimal State (Continuous)

$$\mathbf{x}^{(k+1)} = \underset{\mathbf{x} \in \mathcal{X}}{\operatorname{arg \, max}} \ f(\mathbf{x}, \mathcal{E}^{(k+1)}, \mathcal{T}^{(k+1)})$$

**X** Current Optimal State (Discrete)

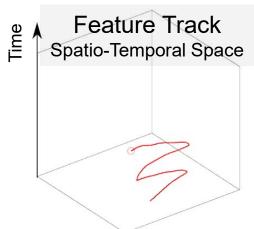
$$\mathbf{x}^{(k+1)} = \underset{\mathbf{x} \in \mathcal{H}(\mathbf{x}^{(k)}) \subset \mathcal{X}}{\arg \max} f(\mathbf{x}, \mathcal{E}^{(k+1)}, \mathcal{T}^{(k+1)})$$

Set of hypothetical states: {Null, North, East, South, West}

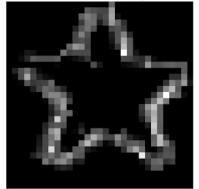




# Feature Tracking with Asynchronous Hypotheses Evaluation



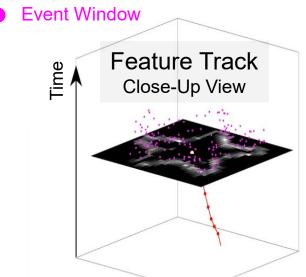
Model  $\mathcal{M}(\mathbf{x},\mathcal{E})$ 



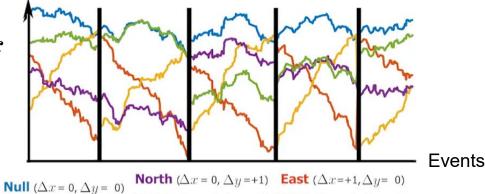
Template  ${\mathcal T}$ 



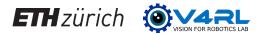




Alignment Score f per hypothesis



**South** ( $\Delta x$  = 0,  $\Delta y$  =+1) **West** ( $\Delta x$  =-1,  $\Delta y$  = 0)



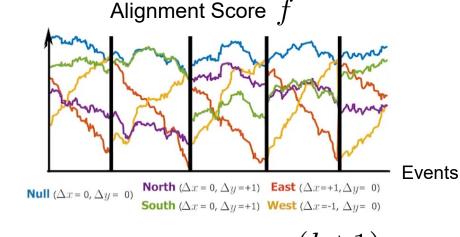
### Feature Tracking with Incremental Alignment Score

For **hypothesis**  $\mathbf{X}_h$ 

with alignment score 
$$f^{(k)} = f(\mathbf{x}_h, \mathcal{E}^{(k)}, \mathcal{T}^{(k)})$$

New event is generated  $e_{k+1}$ 

Update Event Window 
$$\mathcal{E}^{(k)} o \mathcal{E}^{(k+1)}$$
 Template  $\mathcal{T}^{(k)} o \mathcal{T}^{(k+1)}$ 



alignment score must be revaluated  $f^{(k+1)}$  in [Alzugaray & Chli, 3DV'19]

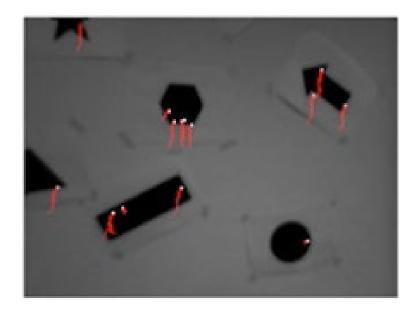
**Incremental Alignment Score** update:

$$f^{(k+1)} = g(f^{(k)}, \mathbf{e}_{k+1})$$

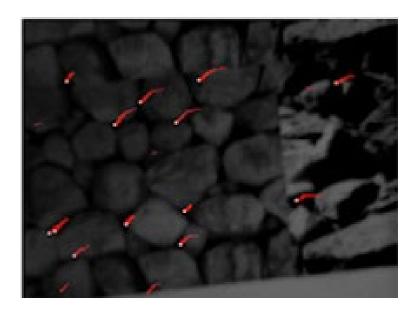


# Asynchronous Multi-Hypothesis Tracking of Events

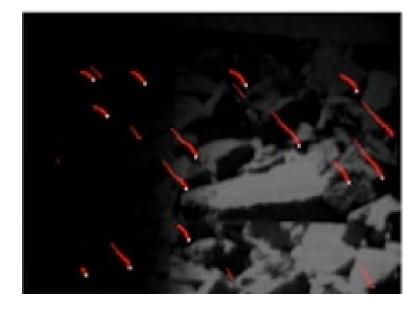
Simple Scene



High-Textured Scene



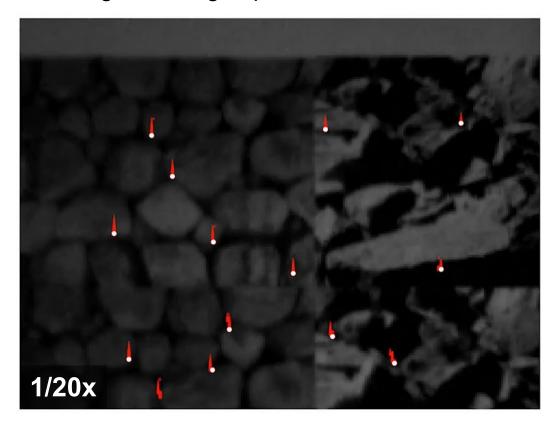
**HDR Illumination** 



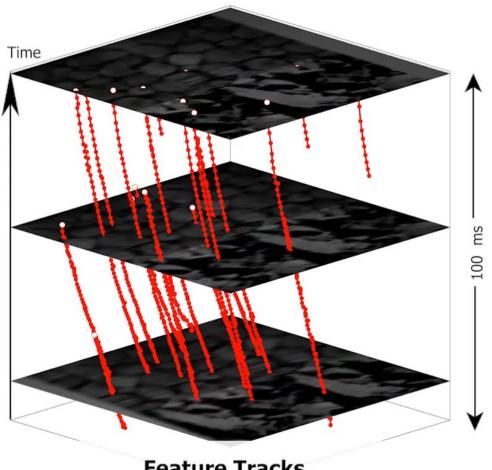


### Asynchronous Multi-Hypothesis Tracking of Events

Tracking under high-speed camera motion



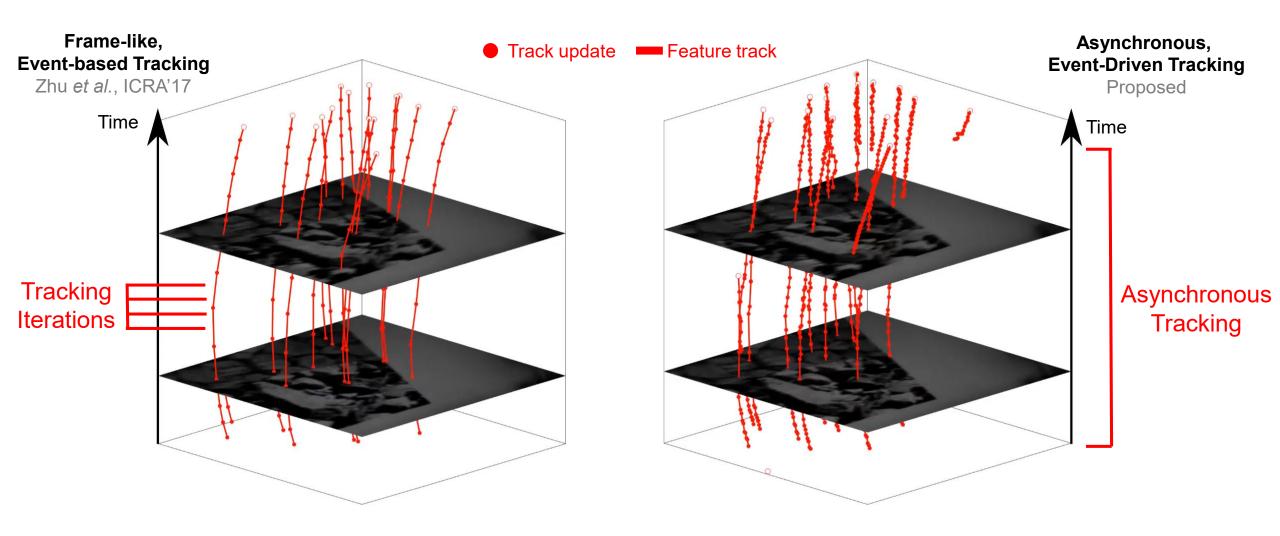
**Feature Tracks** in image space



**Feature Tracks** in spatio-temporal space

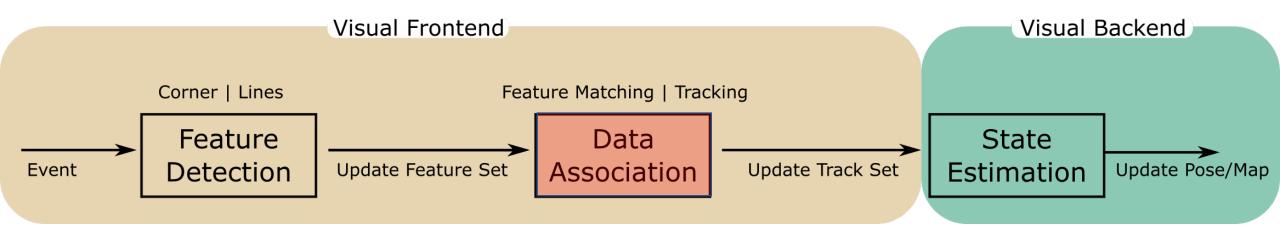


# Asynchronous Event-Driven Feature Tracking





### Asynchronous Event-Driven SLAM Pipeline



- Event Corner Detection
- Naïve Event Corner Association
- Offline Corner Tracks Retrieval

Asynchronous Corner Detection and Tracking for Event Cameras in Real-Time [Alzugaray & Chli, RAL'18]

- Local Event Descriptor
- Multi-hypothesis Data Association
- Online Corner Track Retrieval

ACE: An Efficient Asynchronous Corner Tracker for Event Cameras [Alzugaray & Chli, 3DV'18]

- Hypothesis-based Optimization Framework
- Tracking directly on Raw Events
- Not Real-Time

Asynchronous Multi-Hypothesis
Tracking of Features with Event Cameras
[Alzugaray & Chli, 3DV'19]

- Incremental Hypothesis-based Optimization
- Real-time capabilities.

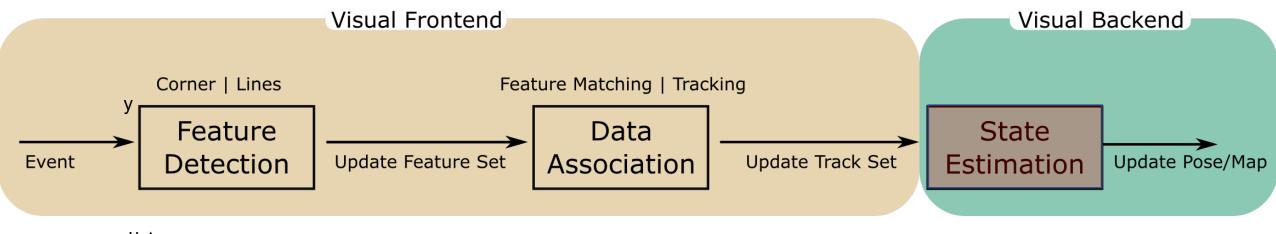
HASTE: multi-Hypothesis Asynchronous Speeded-up Tracking of Events [Alzugaray & Chli, BMVC'20]

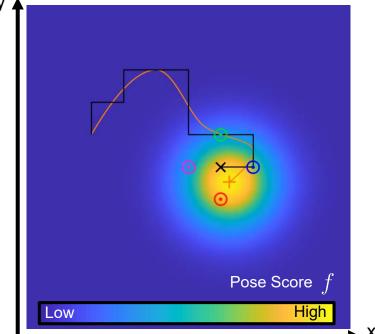
Publicly available:

github.com/ialzugaray/arc\_star\_ros github.com/ialzugaray/haste



### Asynchronous Event-Driven SLAM Pipeline





- Hypothesis-based Optimization Framework
- Tracking directly on Raw Events
- Not Real-Time

**Asynchronous Multi-Hypothesis Tracking of Features with Event Cameras** 

[Alzugaray & Chli, 3DV'19]

- Incremental Hypothesis-based Optimization
- Real-time capabilities.

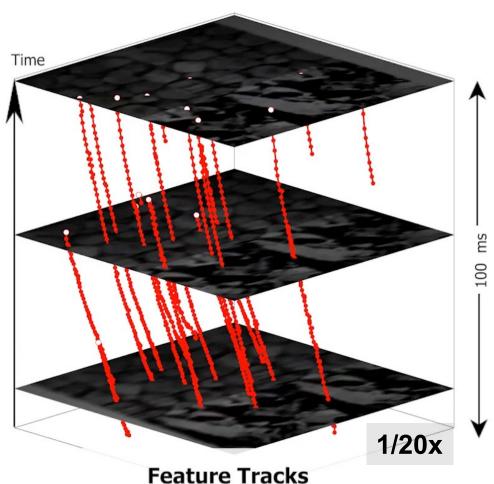
**HASTE:** multi-Hypothesis Asynchronous **Speeded-up Tracking of Events** 

[Alzugaray & Chli, BMVC'20]



### On Event-Driven Perception

- Natural to event cameras
  - Exploit Sparsity & Asynchronicity
- Reduce the number of assumptions
  - Motion-speed tuning / Event-window tuning
- Algorithms require careful design
  - Efficiency / Robustness / Scalability



in spatio-temporal space